

第十五章：气体定律 (2003年—2017年)

选择题

$$\textcircled{1} \quad P = 76 \text{ cmHg} + 20 \text{ cmHg} \\ = 96 \text{ cmHg}$$

B

$$\textcircled{2} \quad \frac{\downarrow V_A}{V_A} = \frac{V_B}{\uparrow T_B} \uparrow$$

A

$$\textcircled{3} \quad PV = nRT$$

A

$$\textcircled{4} \quad \frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\frac{1.5 \times 1 \times 10^5 \times 2.8 \times 10^{-3}}{(273+69)} = \frac{1 \times 10^5 \times V_2}{(10+273)}$$

$$V_2 = 3.35 \times 10^{-3} \text{ m}^3$$

C

$$\textcircled{5} \quad P_1 V_1 = P_2 V_2$$

$$P_1 (A \times h_1) = P_2 (A \times h_2)$$

$$(76+5) \times 94 = (76-5) h_2$$

$$h_2 = 16 \text{ cm}$$

D.

$$\textcircled{6} \quad \frac{V_1}{T_1} = k$$

$$V_1 = k T_1$$

C

$$\textcircled{7} \quad P_1 V_1 = P_2 V_2$$

$$P_1 (A h_1) = P_2 (A h_2)$$

$$(75-15) \times 12 = 75 h_2$$

$$h_2 = 9.6 \text{ cm}$$

B.

$$\textcircled{8} \quad a \rightarrow d \quad (\text{定容过程}, \frac{\uparrow P}{\uparrow T} = k, \text{压强增大})$$

$$b \rightarrow d \quad (\frac{V}{T} = k, \text{定压过程})$$

$$c \rightarrow d \quad (\text{定温过程}, \downarrow PV \uparrow = k, \text{压强减少})$$

B

$$\textcircled{9} \quad \uparrow PV \uparrow = \bar{n} \bar{R} T \uparrow$$

C

$$\textcircled{10} \quad \frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\frac{150 \times 2}{(20+273)} = \frac{250 \times V_2}{(30+273)}$$

$$V_2 = 9.24 \text{ m}^3$$

\textcircled{11}

作答題

$$\textcircled{1} \quad \frac{P_1}{T_1} = \frac{P_2}{T_2}$$

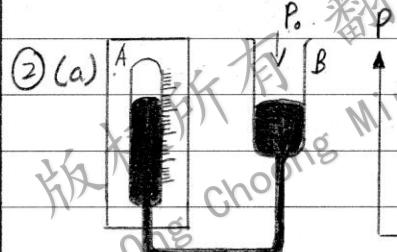
$$\frac{P_1}{T_1} = \frac{P_1 + \frac{1}{100} P_1}{T_1 + S}$$

$$\frac{P_1}{T_1} = \frac{101}{100} \frac{P_1}{T_1 + S}$$

$$T_1 + S = \frac{101}{100} T_1$$

$$\frac{1}{100} T_1 = S$$

$$T_1 = 500 \text{ K}$$



记录 A、B 两管水银面的刻度，测出空气柱长度 L_1 ，此时空气压强即为大气压强 P_0 。提高或降低 B 管，A 管水银面达到另一刻度 M_1 ，而 B 管水银面达到另一刻度 N_1 ，空气柱的长度为 L_2 ，空气压强 $P_1 = P_0 + M_1 N_1$ 。记录 5 组相应的空气柱长度 L 及压强 P 。

$$(b) (i) P = 76 \text{ cmHg} - 70 \text{ cmHg} \\ = 6 \text{ cmHg} \#$$

$$(ii) P_1 V_1 = P_2 V_2$$

$$P_1 (\cancel{A} h_1) = P_2 (\cancel{A} h_2)$$

$$6 \times 30 = P_2 (100 - 68)$$

$$P_2 = 5.625 \text{ cmHg}$$

$$\therefore P = 68 \text{ cmHg} + 5.625 \text{ cmHg} \\ = 73.6 \text{ cmHg} \#$$

$$(iii) \frac{P_1}{T_1} = \frac{P_2}{T_2}, V \text{ 是固定}$$

$$\frac{6}{273+273} = \frac{P_2}{273-3}$$

$$P_2 = 5.4 \text{ cmHg}.$$

$$P = 5.4 \text{ cmHg} + 70 \text{ cmHg} \\ = 75.4 \text{ cmHg.} \#$$

③ (a) 一种气体，不管其压强、温度的高低，总是完全遵守这些简单的规律，这种气体就称作理想气体。

理想气体状态方程式：

$$PV = nRT$$

P = 气体的压强

V = 气体的体积

n = 摩尔数

R = 气体常数

T = 温度

$$(b) (i) F_1 = F_2.$$

$$P_1 A_1 = P_2 A_2$$

$$\frac{P_1 R T_1}{A_1 l_1} A_1 = \frac{P_2 R T_2}{A_2 l_2} A_2$$

$$\frac{n_1}{n_2} = \frac{T_2}{T_1}$$

$$= \frac{400 \times 35}{70 \times 300}$$

$$(ii) I: \frac{P_1}{T_1} = \frac{P_2}{T_2} \quad II: \frac{P_1}{T_1} = \frac{P_2}{T_2}$$

$$P_2 = \frac{T_2}{T_1} \times P_1$$

$$= \frac{330}{300} P_1$$

$$= \frac{550}{400} P_1$$

$\frac{550}{400} P_1 > \frac{330}{300} P_1$, 区域I的压强大于区域II的压强，所以活塞将会往左移动。

(iii) 设活塞向左移动 x.

$$F'_I = F'_II$$

$$P'_I A_I = P'_II A_{II}$$

$$\frac{n_I R T_I}{A_I l_I} A_I = \frac{n_{II} R T_{II}}{A_{II} l_{II}} A_{II}$$

$$\frac{n_I}{n_{II}} = \frac{l_I}{l_{II}}$$

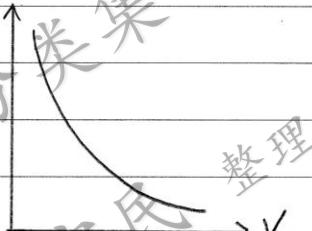
$$\frac{2}{3} = \frac{550 \times (l_I - x)}{330 \times (l_I + x)}$$

$$\frac{2}{3} = \frac{550 \times (35 - x)}{330 \times (70 + x)}$$

$$660 (70 + x) = 1650 (35 - x)$$

$$x = 5 \text{ cm.} \#$$

(4) (a). P



一定的气体，在温度不变的情况下，它的压强跟体积成反比。

(b). 0°C 压强为 P_1

14°C 压强为 P_2

15°C 压强为 P_3

$$\frac{P_1}{T_1} = \frac{P_2}{T_2}$$

$$\frac{P_1}{T_1} = \frac{P_3}{T_3}$$

$$\frac{P_1}{273} = \frac{P_2}{14+273}$$

$$\frac{P_1}{273} = \frac{P_3}{15+273}$$

$$P_2 = \frac{41}{39} P_1$$

$$P_3 = \frac{96}{91} P_1$$

$$P_3 - P_1 = \frac{96}{91} P_1 - \frac{41}{39} P_1 = \frac{1}{273} P_1 \#$$

$$\begin{aligned}
 (c) \quad P_1 V_1 &= P_2 V_2 \\
 75 \times 100 &= [75 + (50-h)] (100-h) \\
 7500 &= (125-h)(100-h) \\
 7500 &= 12500 - 125h - 100h + h^2 \\
 0 &= h^2 - 225h + 5000 \\
 h &= 25 \text{ cm} \#.
 \end{aligned}$$

$$\begin{aligned}
 (d) \quad PV &= nRT \\
 PV &= \frac{m}{M} RT \\
 m &= \frac{PV M}{RT} \\
 &= \frac{1.37 \times 10^3 \times 0.0566 \times 32}{8.31 \times (27+273)} \\
 &= 9.95 \times 10^3 \text{ g} / 9.95 \text{ kg}.
 \end{aligned}$$

$$\begin{aligned}
 (6) \quad \frac{P_A}{V_A} &= \frac{P_B}{V_B} \\
 \frac{n_A R T_A}{V_A} &= \frac{n_B R T_B}{V_B} \\
 \frac{V_B}{V_A} &= \frac{n_B T_B}{n_A T_A} \\
 &= \frac{(7+273)}{(27+273)} \times \frac{n_B}{n_A} \\
 &= \frac{14}{15} \times \frac{n_B}{n_A} / 0.933 \frac{n_B}{n_A} \#
 \end{aligned}$$

$$\begin{aligned}
 P'_A &= P'_B \\
 \frac{n_A R T_A}{V'_A} &= \frac{n_B R T_B}{V'_B} \\
 \frac{V'_B}{V'_A} &= \frac{n_B T_B}{n_A T_A} \\
 &= \frac{(17+273)}{(42+273)} \times \frac{n_B}{n_A} \\
 &= \frac{58}{63} \times \frac{n_B}{n_A} / 0.921 \frac{n_B}{n_A} \#
 \end{aligned}$$

(5) (a) 完全遵守压强、体积及温度间的变化规律的气体，称为理想气体。

$$\begin{aligned}
 (b) \quad \text{斜率} &= \frac{y_2 - y_1}{x_2 - x_1} \\
 \frac{y_B - 1.2}{300 - 0} &= \frac{1.2 - 0}{0 + 273} \\
 y_B &\approx 2.52 \\
 V_B &= 2.52 \text{ m}^3 \#
 \end{aligned}$$

$$\begin{aligned}
 PV &= nRT \\
 P_B \times 2.52 &= 0.5 \times 8.31 \times (300 + 273) \\
 P_B &= 945.26 \text{ Pa} \#.
 \end{aligned}$$

$$\begin{aligned}
 (c) (i) (ii) \quad P_0 V_0 &= P_1 V_1 \\
 76 \times 50 &= (76+h)h \\
 3800 &= 76h + h^2 \\
 0 &= h^2 + 76h - 3800 \\
 h &= 34.42 \text{ cm}.
 \end{aligned}$$

$$\begin{aligned}
 \therefore h &= 34.42 \text{ cm} \# ; P_1 = 76 \text{ cmHg} + 34.42 \text{ cmHg} \\
 &= 110.42 \text{ cmHg} \#
 \end{aligned}$$