

## CHAPTER 3. FRACTIONS (分数)

$$\frac{a}{b} = a \div b, b \neq 0$$

$$\text{Fraction} = \frac{\text{Numerator}}{\text{Denominator}}$$

### Example 1: Equivalent Fractions

$$\frac{1}{2} = \frac{2}{4} = \frac{3}{6} = \frac{4}{8}$$

$$\frac{a}{b} = \frac{a \times c}{b \times c} = \frac{a \div c}{b \div c}, b \neq 0, c \neq 0$$

### Example 2:

Express  $\frac{5}{12}$  and  $\frac{4}{9}$  to a common denominator.

Solution: LCM of 12 and 9 is 36.

$$\frac{5}{12} = \frac{5 \times 3}{12 \times 3} = \frac{15}{36} \qquad \frac{4}{9} = \frac{4 \times 4}{9 \times 4} = \frac{16}{36}$$

- ❖ Proper Fraction = A fraction whose numerator is less than its denominator. ( $\frac{3}{4}$ )
- ❖ Improper Fraction = A fraction whose numerator is greater than or equal to the denominator. ( $\frac{8}{5}$  and  $\frac{9}{9}$ ).
- ❖ Mixed Number = A number that contains an integer part and a fractional part. ( $1\frac{7}{10}$ )

$$\frac{\text{dividend (numerator)}}{\text{divisor (denominator)}} = \text{quotient} + \frac{\text{remainder}}{\text{divisor}}$$

### Example 3:

Express  $\frac{37}{14}$  as a mixed number.

$$\text{Solution: } \frac{37}{14} = 2\frac{9}{14}$$

### Comparing Fractions

- Same denominators, compare the numerators. ( $\frac{5}{8}$  and  $\frac{3}{8}$ )
- Same numerators, compare the denominators. ( $\frac{2}{3}$  and  $\frac{2}{5}$ )
- Different denominators, make the denominators the same before comparing.  
( $\frac{4}{7}$  and  $\frac{3}{8}$ )

### Addition and Subtraction of fractions

$$\frac{a}{c} + \frac{b}{c} = \frac{a+b}{c} \qquad \text{and} \qquad \frac{a}{c} - \frac{b}{c} = \frac{a-b}{c}$$