

Trigonometry Revision

1. Solve these equations for $0^\circ \leq x \leq 360^\circ$
 - a. $4 \sin x = 3$
 - b. $5 \tan x - 1 = 9$
 - c. $6 \cos x + 5 = 8$
 - d. $8 \sin(x + 20) = 5$
 - e. $10 - 3 \cos x = 9$
 - f. $9 \sin(x - 15) = -4$
2. In the following equations find all the values of θ between 0° and 360°
 - a. $\cos \theta = 0.776$
 - b. $\sin 2\theta = -0.364$
 - c. $\tan 3\theta = 1.988$
 - d. $\cos \frac{\theta}{2} = -0.379$
 - e. $\tan \frac{\theta}{2} = -1.030$
 - f. $\sin \frac{3\theta}{2} = 0.664$
3. Solve the following equations for $0 \leq x \leq 2\pi$
 - a. $3 \tan x + 2 = 5$
 - b. $\sin(x - \frac{\pi}{6}) = \frac{\sqrt{3}}{2}$
 - c. $\sin 2x = \frac{1}{2}$
 - d. $6 \cos 3x - 3 = 0$
 - e. $7 - 2 \tan 4x = 13$
 - f. $10 \cos \frac{x}{3} = 1$
4. Solve $6 \cos 30x - 3 = 0$ for $0^\circ \leq x \leq 24^\circ$
5. Solve $3 \tan x = \sqrt{27}$ for $-180^\circ \leq x \leq 180^\circ$
6. Solve $5 + 2 \cos(3\theta - \frac{\pi}{4}) = 6$ for $-\pi \leq x \leq \pi$
7. Simplify
 - a. $\frac{\sin^3 \theta + \sin \theta \cos^2 \theta}{\cos \theta}$
 - b. $\frac{1 + \cos \theta}{\sin \theta} + \frac{\sin \theta}{1 + \cos \theta}$
8. Prove the identity $\frac{\sin \theta}{\tan \theta (1 - \cos \theta)} = \frac{\cos \theta}{1 - \cos \theta}$
9. Express $4 \cos^2 x - \sin^2 x$ in terms of $\cos x$
10. Express in terms of $\sin \theta$
 - a. $\sin^2 \theta - \cos^2 \theta$
 - b. $2 \cos^2 \theta - 4 \sin \theta$
11. Prove $\frac{\sin^4 \theta}{\tan \theta} = \sin \theta \cos \theta - \sin \theta \cos^3 \theta$

12. Prove the following identities
- $\cos^5\theta = \cos\theta - 2\sin^2\theta\cos\theta + \cos\theta\sin^4\theta$
 - $(4\sin\theta + 3\cos\theta)^2 + (3\sin\theta - 4\cos\theta)^2 = 25$
 - $\tan^2 A - \tan^2 B = \frac{\sin^2 A - \sin^2 B}{\cos^2 A \cos^2 B}$
13. Show that $(1 + \sin\theta + \cos\theta)^2 = 2(1 + \sin\theta)(1 + \cos\theta)$
14. Prove
- $\tan\theta = \sqrt{\frac{\sin^2\theta}{1-\sin^2\theta}}$
 - $\frac{1-\sin^2\theta}{\tan\theta} = \frac{\cos^3\theta}{\sin\theta}$
 - $\frac{\sin^2\theta}{1-\cos\theta} = 1 + \cos\theta$
 - $(2 - \cos^2\theta)^2 - 4\sin^2\theta = \cos^4\theta$
- 15.
- Express $2\cos x - \sin^2 x$ in the form $(\cos x + p)^2 + q$, stating the values of p and q
 - Use your answer to part (a) to find the maximum and minimum values of $2\cos x - \sin^2 x$
16. Use the identity $\sin^2 x + \cos^2 x = 1$ to prove that $\frac{1+\sin x \cos x}{\cos^2 x} = \tan^2 x + \tan x + 1$
17. Use the identity you proved in part (a) to find minimum values of $\frac{1+\sin x \cos x}{\cos^2 x}$
18. Solve $\sqrt{3}\sin x - \cos x = 0$ for $0 \leq x \leq 2\pi$
19. Solve the equation $2\cos^2 x = 1 - \sin x$ for $0^\circ \leq x \leq 360^\circ$
20. Solve the equation $\sin^2(2x - 60^\circ) = 0.6$ for $0^\circ \leq x \leq 180^\circ$
21. Solve the equations for $0^\circ \leq \theta \leq 360^\circ$
- $\cos^2\theta - \sin^2\theta = 0$
 - $2\cos^2\theta + \sin\theta = 1$
 - $3\sin^2\theta = \cos^2\theta$
 - $\cos^2\theta - 4\sin^2\theta = 1$
 - $1 + \sin\theta \cos^2\theta = \sin\theta$
 - $6\sin(\theta + 70)^\circ - 5\cos(\theta + 70)^\circ = 0$
 - $3\cos 2\theta = 4\sin 2\theta$
 - $2\sin\theta = 3\tan\theta$
22. Solve the equation $\sin\theta + 5\cos\theta = 3\sin\theta$ for $0 \leq x \leq 2\pi$
- 23.
- Simplify $\frac{6-6\cos^2\theta}{2\sin\theta}$
 - Hence solve the equation $6 - 6\cos^2\theta = 3\sin\theta$ for $0 \leq x \leq 2\pi$
24. Solve the equation $\tan^3\theta - \tan^2\theta - 2\tan\theta = 0$ for $0^\circ \leq x \leq 180^\circ$